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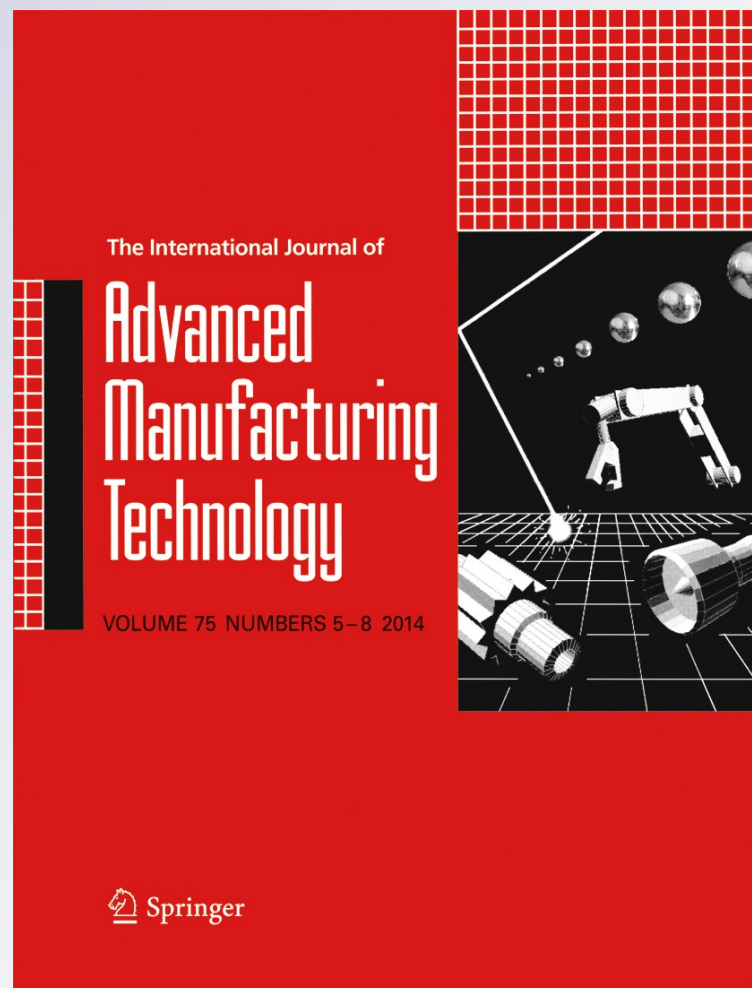
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# Investigations on the chip formation mechanism and shear localization sensitivity of high-speed machining Ti6Al4V

Bing Wang · Zhanqiang Liu

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**Abstract** This study develops a combined numerical and experimental approach to get deeper insights into chip formation mechanism for high-speed machining of titanium alloy Ti6Al4V. The numerical investigation of high-speed machining is implemented with the aid of finite element analysis software Abaqus/Explicit, in which the Johnson-Cook (JC) fracture model with an energy-based ductile failure criterion is adopted. Meanwhile, the experiments of high-speed orthogonal cutting are carried out to validate the numerical results. The cutting speeds are selected ranging from 50 to 3,000 m/min, and the uncut chip thickness is fixed at 0.1 mm. The variables investigated include the serrated degree and serrated frequency of chips in addition to the cutting force. The results show that both the serrated degree and serrated frequency have positive correlations with the cutting speed. An important regularity for the transformation of chip morphology from serrated to unit at a critical cutting speed has been achieved, and the critical value for Ti6Al4V is about 2,500 m/min. The research also finds that the cutting force decreases with the increasing cutting speed, while its fluctuant frequency and amplitude increase sharply. Furthermore, the influences of JC fracture constants (the five constants in JC fracture model) on chip formation are investigated based on the finite element

method, which is the main original and innovative highlight of this study. The shear localization sensitivity is firstly proposed to describe the influences of JC fracture constants on the chip formation process. When the JC fracture constants decrease, the shear localization sensitivity is positive which means that the serrated degree increases and vice versa. The sensitivity analyses indicate that the influences of initial failure strain  $D_1$  and exponential factor of stress triaxiality  $D_2$  on chip formation process are more conspicuous than the rest three ones. This paper is enticing from both the engineering and the analytical perspectives aimed at predicting the evolution of serrated chip formation and chip morphology transformation in metal cutting process.

**Keywords** Finite element method · JC fracture model · Shear localization sensitivity · High-speed machining · Ti6Al4V

## Nomenclature

$A$	Initial yield stress (MPa)
$a_c$	Uncut chip thickness (mm)
$B$	Hardening modulus (MPa)
$C$	Strain rate dependency coefficient
$d$	Pitch of two neighboring trapezoids in serrated chips (mm)
$D$	Damage variable
$d_1$	Diameter of slot milling cutter (mm)
$d_2$	Width of workpiece (mm)
$D_1$	Initial failure strain of JC fracture model
$D_2$	Exponential factor of JC fracture model
$D_3$	Triaxiality factor of JC fracture model
$D_4$	Strain rate factor of JC fracture model
$D_5$	Temperature factor of JC fracture model
$f$	Chip serrated frequency

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$G_f$	Fracture energy required to form a unit area of crack (J)
$G_s$	Chip serrated degree
$G_s^{D_i}$	Chip serrated degree under different fracture constants
$G_s^{\text{original}}$	Chip serrated degree under the original fracture constants
$h$	Discontinuous section height of serrated chip (mm)
$H$	Maximum height of serrated chip (mm)
$L$	Characteristic length to determine the stress-displacement response (mm)
$m$	Thermal softening coefficient
$n$	Strain hardening coefficient
$P$	Average of three normal stresses, also called the hydrostatic pressure (MPa)
$S$	Shear localization sensitivity of serrated chip
$T$	Temperature at a given calculation instant (K)
$T_m$	Melting temperature of workpiece material (K)
$T_r$	Room temperature (K)
$\bar{u}$	Equivalent plastic displacement (mm)
$\bar{u}_f$	Equivalent plastic displacement at fracture (mm)
$V$	Cutting speed (m/min)
$w$	Damage initiation parameter
$\bar{\varepsilon}$	Equivalent plastic strain
$\bar{\varepsilon}_0$	Initial plastic strain
$\dot{\bar{\varepsilon}}$	Equivalent strain rate ( $\text{s}^{-1}$ )
$\dot{\bar{\varepsilon}}_0$	Reference strain rate ( $\text{s}^{-1}$ )
$\bar{\varepsilon}_f$	Equivalent strain at fracture
$\Delta\bar{\varepsilon}$	Increment of equivalent plastic strain
$\bar{\sigma}$	Equivalent stress (MPa)
$\sigma_y$	Yield stress (MPa)

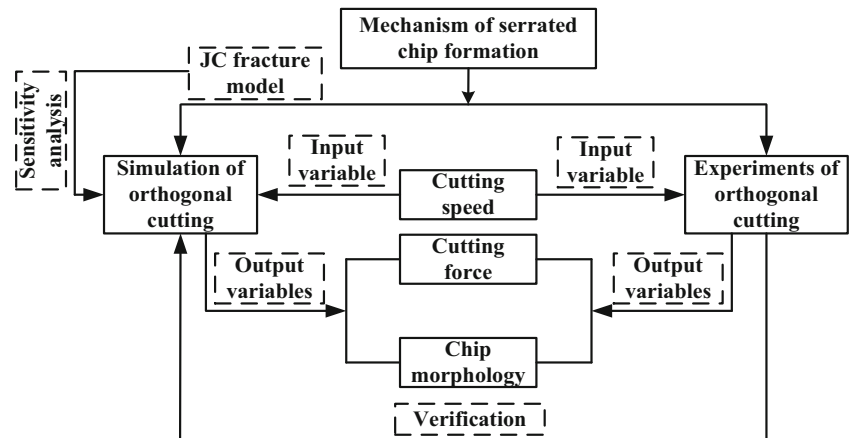
## 1 Introduction

Titanium alloys have excellent properties such as high specific strength (strength-to-weight ratio), high toughness, high temperature resistance, corrosion resistance, etc. These admirable properties make titanium alloys bear high load and maintain sufficient strength at elevated temperature [1–3]. Therefore, the titanium alloys have been applied in the automotive and aerospace industries, medical equipments and implants, chemical processing components, power stations, nuclear and marine applications, etc. [4]. As the same as other materials, titanium alloys should be subjected to manufacturing operations before entering into service. The machining process is one of the most important manufacturing processes due to the superior surface quality added to the finished products. Most mechanical components made from titanium alloys are still fabricated by conventional machining processes such as turning, milling, drilling, grinding, boring, and reaming.

However, the utilization of titanium alloys is restricted by their poor machinability. Hitherto, many researchers have paid attention to the investigations on machining mechanism of titanium alloys, which includes chip formation mechanism [5], cutting force and cutting temperature [6], finished surface quality [7], tool wear and tool failure [8], etc. Due to the unique properties of titanium alloys, especially for their poor thermal property, the chips produced are serrated even when the cutting speed is very low, which is distinctly different from other materials. As the chip formation has great effect on the variation of cutting force, the distribution of cutting temperature in addition to the tool wear and tool failure, it is important to have deeper insights into the essential factors which control the chip formation mechanism. Many researches have paid attention to the formation mechanism of serrated chips, which can mainly be summarized as adiabatic shear theory [9–11] and periodic crack theory [12–14]. The chip formation is dominated by the material properties and mechanical conditions during the cutting process, in which the material undergoes severe deformation within the primary shear zone. However, the dynamic mechanical behavior of materials under the coupling influences of large strains, high strain rates, and elevated temperatures is still poorly understood, and the relevant theoretical analyses are difficult to proceed. It is more convenient and feasible to analyze the material behavior during chip formation process based on finite element method.

Previously, several different numerical methods were used to simulate serrated chip formation. These methods were based on either implicit or explicit software packages such as Deform [15], Ansys [16], Abaqus [17], Forge [18], Advantedge<sup>TM</sup> [19], SPH [20], etc. Various models have been developed involving different meshes, plasticity models, and fracture models, which mainly include strain-based fracture criterion, the Johnson-Cook (JC) fracture model, the Cockcroft-Latham fracture criterion, and without fracture criterion [21–24]. To accurately conduct the research of cutting process based on finite element method, the reasonable selection of material constitutive model under severe loading conditions is prerequisite and of vital importance. In addition, the success and reliability of numerical analyses are heavily dependent on the material flow stress, the friction parameters between the tool–chip interface, the mechanical and thermal parameters, and the material separation criterion [25, 26]. In consideration of the mechanical characteristics and deformation status during metal cutting process, the JC constitutive model and JC fracture model are most widely used, which take the coupling effects of strain, strain rate, and temperature into account. Recently, cutting simulations have been performed more precisely and realistically by incorporating progressive failure model with chip separation criterion or adaptive meshing method into the finite element analyses [27, 28]. The most important factor in the progressive failure model is

**Fig. 1** Outline of this study

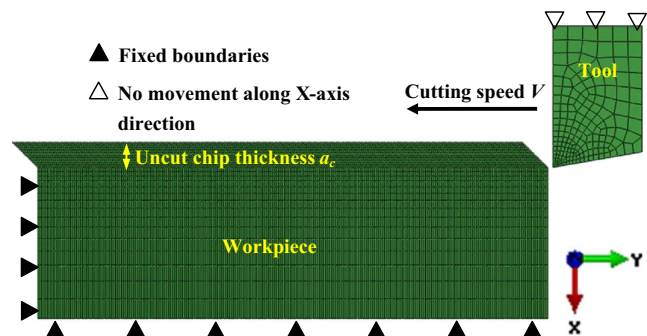


to properly implant the damage evolution criterion into the failure model. There are two ways applied to determine the damage evolution in Abaqus software which are defined as the equivalent plastic displacement and fracture energy dissipation. Ambati and Yuan [29] researched the mesh dependence in cutting simulation based on the plastic displacement damage evolution criterion with exponential softening. Their results demonstrate that the effect of element size on computational results is reduced significantly if the failure criterion in the process simulation is controlled by a characteristic element length considered from the progressive damage model. Umbrello [30] conducted the finite element analyses of cutting force, chip morphology, and segmentation during conventional and high-speed machining Ti6Al4V, in which three JC constitutive equations with different sets of material constants were implemented. The results indicate that a good prediction of both principal cutting force and chip morphology can be achieved only if the material constants for the JC constitutive equation adopted are reasonable. Hosseini and Kazeminezhad [31] proposed a new and better constitutive model in finite element method to investigate the material behavior during intense deformation. The model is completely based on physical mechanism that can predict all stages of flow stress evolution and also can elucidate the effects of strain and strain rate on flow stress evolution of material during intense plastic deformation which can be used in the simulation of high-speed machining. There are also other scholars who have investigated the metal cutting process with the aid of finite element method in such aspects as chip morphology [32, 33], burr formation [34], orthogonal micro-machining process [20], etc.

There has been a considerable amount of research to study the serrated chip formation mechanism of titanium alloys depending on the finite element simulation of machining, in which different material failure models have also been implanted. Nevertheless, the influences of different material fracture models, especially the influences of fracture model

parameters, have not yet been understood completely. Because the material fracture process involves the roles of strain, strain rate, and temperature, it is also important to investigate the different influences of these three variables. Research of the influences of fracture model parameters on the chip formation process can help to understand the essence of chip deformation or fracture under different cutting parameters.

The main objective of this paper concerns the presentation of numerical and experimental analyses for orthogonal cutting process in order to get deeper insights into the mechanism of serrated chip formation. Figure 1 illustrates the outline of the research. One aim of this research is to conduct the comparison between the numerical and the experimental results with respect to the cutting force and chip morphology under different cutting conditions, which can validate the reliability of the numerical analyses. Then, the chip morphology and serrated degree are analyzed through the finite element simulation with different JC fracture constants. In addition, the concept of shear localization sensitivity is proposed to investigate the influences of JC fracture constants on the chip formation process. This novel concept can help to evaluate the influences of JC fracture constants on the chip formation quantitatively. Consequently, the control mechanism of material property on the chip formation is further revealed. Among all



**Fig. 2** Schematic of finite element model for orthogonal cutting



**Table 1** JC constitutive model parameters of Ti6Al4V [37]

$A$ (MPa)	$B$ (MPa)	$n$	$C$	$m$
862	331	0.34	0.012	0.8

titanium alloys, Ti6Al4V is the most widely used and so it has been chosen as the workpiece material in this research.

## 2 Finite element method and modeling procedure

The finite element analysis software Abaqus/Explicit was adopted to simulate the two-dimensional orthogonal cutting process of Ti6Al4V. The process of serrated chip formation was analyzed after modeling the tool, workpiece, relevant properties of materials, contact, and boundary conditions. Through analyses of cutting process under different fracture model parameters, the shear localization sensitivity of serrated chips to fracture model parameters in machining Ti6Al4V is deduced, which can help to improve the comprehension of serrated chip formation mechanism.

### 2.1 Modeling of orthogonal cutting

The numerical method developed with Abaqus/Explicit was adopted because it can avoid the convergence caused by the contact and material complexities [35]. The finite element model was established by using the planar quadrilateral continuum elements (CPE4RT) which are suitable for the coupled temperature-displacement calculation and have reduced integration and hourglass control features. An element deletion technique was used to allow element separation to form chip. Once the nodes in element reach the degradation value of 1, it is separated and excluded from the computation. Cutting tool is constrained as a rigid body and its rake angle is  $0^\circ$ . The cutting speeds  $V$  are set from 50 to 3,000 m/min which are parallel to the workpiece as shown in Fig. 2. Workpiece is fixed in bottom and left sides against both vertical and horizontal movements. The uncut chip thickness  $a_c$  is set at 0.1 mm which is kept constant for all simulations. Contact definition between cutting tool and workpiece is defined by using penalty contact model, in which the tool surface is the master one while the chip face is the slave one. So, the mesh

density of the chip layer is larger than that of the tool. The chip–tool friction is based on Coulomb's friction law which is used in many previous researches [17, 32]. A chamfer is designed on the removed material layer to avoid distortion problems at the beginning of calculation.

### 2.2 Constitutive model of Ti6Al4V

In finite element method, accurate material flow stress models are highly essential to describe the workpiece material behavior under high strain rate deformation conditions. The JC constitutive model is considered the most widely in the simulation of high-speed machining because it is a thermal viscoplastic model suitable for conditions where the strain rate is over a large range from  $10^2$  to  $10^6 \text{ s}^{-1}$  [36]. The effects of strain hardening, strain rate hardening, and thermal softening are taken into account simultaneously. The JC constitutive model is expressed by Eq. (1).

$$\bar{\sigma} = \underbrace{\left[ A + B\bar{\epsilon}^n \right]}_{\text{Elastoplastic term}} \underbrace{\left[ 1 + C \ln \left( \frac{\dot{\bar{\epsilon}}}{\dot{\bar{\epsilon}}_0} \right) \right]}_{\text{Viscosity term}} \underbrace{\left[ 1 - \left( \frac{T - T_r}{T_m - T_r} \right)^m \right]}_{\text{Thermal softening term}} \quad (1)$$

where  $\bar{\sigma}$  is the equivalent stress,  $\bar{\epsilon}$  is the equivalent plastic strain,  $\dot{\bar{\epsilon}}$  is the equivalent strain rate,  $\dot{\bar{\epsilon}}_0$  is the reference strain rate. The parameters  $T$ ,  $T_m$ , and  $T_r$  are current temperature, melting temperature of workpiece material, and room temperature, respectively.  $A$  is the initial yield stress,  $B$  is the hardening modulus,  $n$  is the strain hardening coefficient,  $C$  is the strain rate dependency coefficient, and  $m$  is the thermal softening coefficient. The JC constitutive model parameters and the physical and mechanical properties of Ti6Al4V used to simulate its mechanical behavior are specified in Tables 1 and 2, respectively.

The tools used in the simulations are tungsten carbide inserts whose rake angle and flank angle are  $0^\circ$  and  $10^\circ$ , respectively. The physical parameters of cutting tools are presented in Table 3.

### 2.3 Chip separation criterion

In order to simulate the emergence of chip formation, a fracture model that gives rise to chip detachment is used.

**Table 2** Physical and mechanical properties of Ti6Al4V [24]

Density (kg/m <sup>3</sup> )	Elastic modulus (GPa)	Poisson's ratio	Thermal conductivity (W/m K)	Specific heat (J/kg K)	Thermal expansion coefficient (/K)	Melting temperature (K)
4,430	109 (323 K)	0.34	6.8 (293 K)	611 (293 K)	9.0E-6	1,878
	91 (523 K)		7.4 (373 K)	624 (373 K)		
	75 (723 K)		9.8 (573 K)	674 (573 K)		
			11.8 (773 K)	703 (773 K)		

**Table 3** Physical parameters of the tungsten carbide cutting tools [32]

Density (kg/m <sup>3</sup> )	Elastic modulus (GPa)	Poisson's ratio	Thermal conductivity (W/m K)	Specific heat (J/kg K)
11,900	534	0.22	50	400

The fracture model is established according to the classical cumulative damage law expressed by Eq. (2), in which the JC fracture model [38] has been developed.

$$w = \sum \frac{\Delta \bar{\varepsilon}}{\bar{\varepsilon}_f} \quad (2)$$

where  $\Delta \bar{\varepsilon}$  is the increment of equivalent plastic strain which occurs during an integration cycle and  $\bar{\varepsilon}_f$  is the equivalent strain to fracture under the current conditions of strain rate, temperature, pressure, and equivalent stress. Damage is then allowed to initiate when  $w=1.0$ . The general expression for the JC fracture strain is shown as Eq. (3) [38].

$$\bar{\varepsilon}_f = \left[ D_1 + D_2 \exp \left( D_3 \frac{P}{\bar{\sigma}} \right) \right] \left[ 1 + D_4 \ln \frac{\dot{\bar{\varepsilon}}}{\dot{\bar{\varepsilon}}_0} \right] \left[ 1 + D_5 \frac{T - T_r}{T_m - T_r} \right] \quad (3)$$

where  $P$  is the average of three normal stresses and it is also called the hydrostatic pressure. The ratio of  $\frac{P}{\bar{\sigma}}$  is referred to as the stress triaxiality. It can be seen from Eq. (3) that the fracture strain  $\bar{\varepsilon}_f$  depends on the stress triaxiality, the equivalent strain rate, the temperature, as well as the fracture constants  $D_i$  ( $i=1, 2, 3, 4, 5$ ). The five fracture constants indicate initial failure strain, exponential factor, triaxiality factor, strain rate factor, and temperature factor, respectively. The fracture constants of JC fracture model for Ti6Al4V are presented in Table 4. One main object of this paper is to investigate the influences of JC fracture constants on the chip formation during high-speed machining Ti6Al4V through the simulation with different JC fracture constants. Then, the effects of shear localization sensitivity of serrated chips to JC fracture constants can be deduced.

In this study, an energy-based ductile failure criterion is applied to illustrate the material behavior of damage evolution during high-speed machining [39]. This model defines the fracture energy  $G_f$  as a material parameter which denotes the

energy required to form a unit area of crack. The parameter  $G_f$  is also called Hillerborg's fracture energy. It governs the weakening of workpiece material according to a stress-displacement response after damage initiation rather than a stress-strain response, so it is favorable to reduce the mesh dependency. Hillerborg's fracture energy can be expressed as Eq. (4).

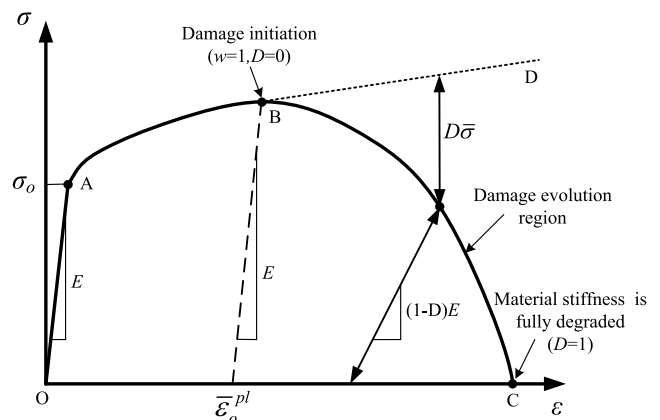
$$G_f = \int_{\bar{\varepsilon}_0}^{\bar{\varepsilon}_f} L \sigma_y d\bar{\varepsilon} = \int_0^{\bar{u}_f} \sigma_y d\bar{u} \quad (4)$$

where  $\bar{\varepsilon}_0$  is the initial plastic strain which is equal to zero before the damage initiates, and  $L$  is the characteristic length. The parameter  $\bar{u}$  is the equivalent plastic displacement as the fracture work conjugate of the yield stress after onset of the damage. The parameter  $\bar{u}_f$  is the equivalent plastic displacement when the fracture occurs. A linear evolution of the damage is assumed, which means that  $\bar{u} = L\bar{\varepsilon}$  after the damage initiation. The damage variable  $D$  can be expressed by Eq. (5).

$$D = \frac{L\bar{\varepsilon}}{\bar{u}_f} = \frac{\bar{u}}{\bar{u}_f} \quad (5)$$

When the damage variable  $D$  reaches 1, the material stiffness is fully degraded, then the relevant elements are deleted and the crack generates.

Figure 3 presents the stress-strain behavior of material undergoing damage evolution [35]. The solid curve OABC



**Fig. 3** Stress-strain response of material damage evolution

**Table 4** The fracture constants of JC fracture model for Ti6Al4V [37]

$D_1$	$D_2$	$D_3$	$D_4$	$D_5$
-0.09	0.25	-0.5	0.014	3.87

illustrates the damaged stress–strain response, while the dashed curve OABD illustrates the stress–strain response assuming there is no damage occurring. The material deformation and fracture process can be divided into three stages as shown in Fig. 3. The first stage OA indicates the linear elastic deformation period. When the stress exceeds the yield stress  $\sigma_0$ , the material enters the second stage AB, in which material undergoes the stable plastic deformation. The effect of strain hardening is prominent in this period. When the cumulative damage parameter  $w$  reaches 1 as the point B shows, the plastic instability initiates which turns on the third stage BC. Afterwards, material enters the stage of failure evolution and the thermal softening takes the priority which results in the decrease of the equivalent stress. When the stress–strain curve extends to point C (i.e., the damage variable  $D$  reaches 1), the material stiffness is fully degraded and the crack emerges.

### 3 Comparison of numerical and experimental results

#### 3.1 Experimental setup of orthogonal cutting

Figure 4 shows the schematic and actual photos of experimental setup for orthogonal cutting. The cutting experiments were conducted on Daewoo ACE-V500 vertical machining center whose spindle rotational speed ranges from 80 to 10,000 r/min. The cutter used in the experiments is Kennametal 4.96164-210 90° SN slot milling cutter whose diameter  $d_1$  is 160 mm. The width of workpiece  $d_2$  is 20 mm as shown in Fig. 4. Because the cutter diameter  $d_1$  is much larger than the workpiece width  $d_2$ , the directions of cutting force and thrust

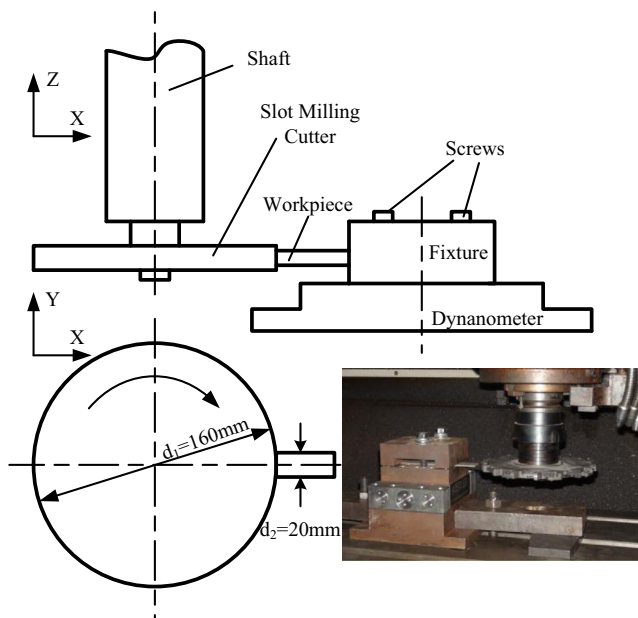


Fig. 4 Experimental setup for orthogonal cutting

force can be regarded as approximately parallel with the coordinate axes  $Y$  and  $X$ , respectively. The insert type is SNHX12L5PZTNGP with coated carbide (KC725M) and its rake angle is  $0^\circ$ . The workpieces were machined at the cutting speeds ranging from 50 to 3,000 m/min, and the feed rate per tooth was fixed at 0.1 mm/z. The feed rate per tooth corresponds to the uncut chip thickness in orthogonal cutting. After each cutting experiment was finished, the insert was replaced by a new one so as to eliminate the influence of tool wear on the experimental results. The axial cutting width is 2.0 mm and the cutting condition is dry cutting. The cutting force was measured by Kistler three-dimensional dynamometer, which was mounted through special fixture on the worktable.

Chips collected after all cutting experiments were inlaid into mosaic materials as specimens, after which the procedures of grinding, polishing, and etching were carried out sequentially. Then, the micrographs of the chips were observed with the aid of VHX-600 ESO digital microscope, by which the relevant geometrical values of chips can be measured.

#### 3.2 Geometric characteristics of serrated chips

The serrated chip formation can be presented by Fig. 5 in a visualized way. The shadow areas refer to three cutting shear zones as primary shear zone, secondary shear zone, and tertiary shear zone. The geometric characteristics of serrated chips are described by the two parameters of serrated degree  $G_s$  and serrated frequency  $f$ , which are expressed by Eqs. (6) [40] and (7) [41], respectively. The serrated chip can be regarded as a sequence of trapezoids arranged periodically, and each trapezoid is formed by two shearing planes. If the pitch of two neighboring trapezoids and the chip sliding velocity are known, the serrated frequency can be deduced by Eq. (7).

$$G_s = \frac{h}{H} \quad (6)$$

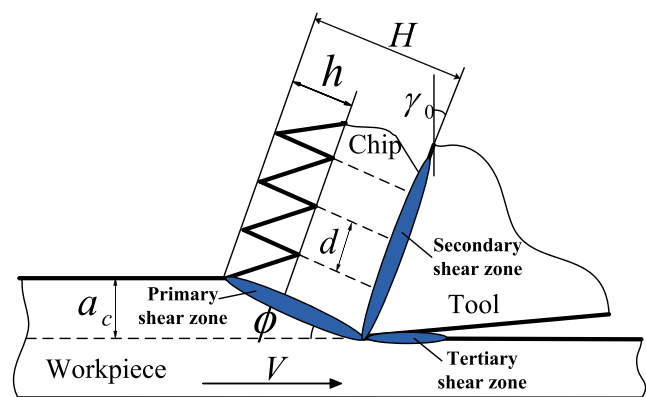
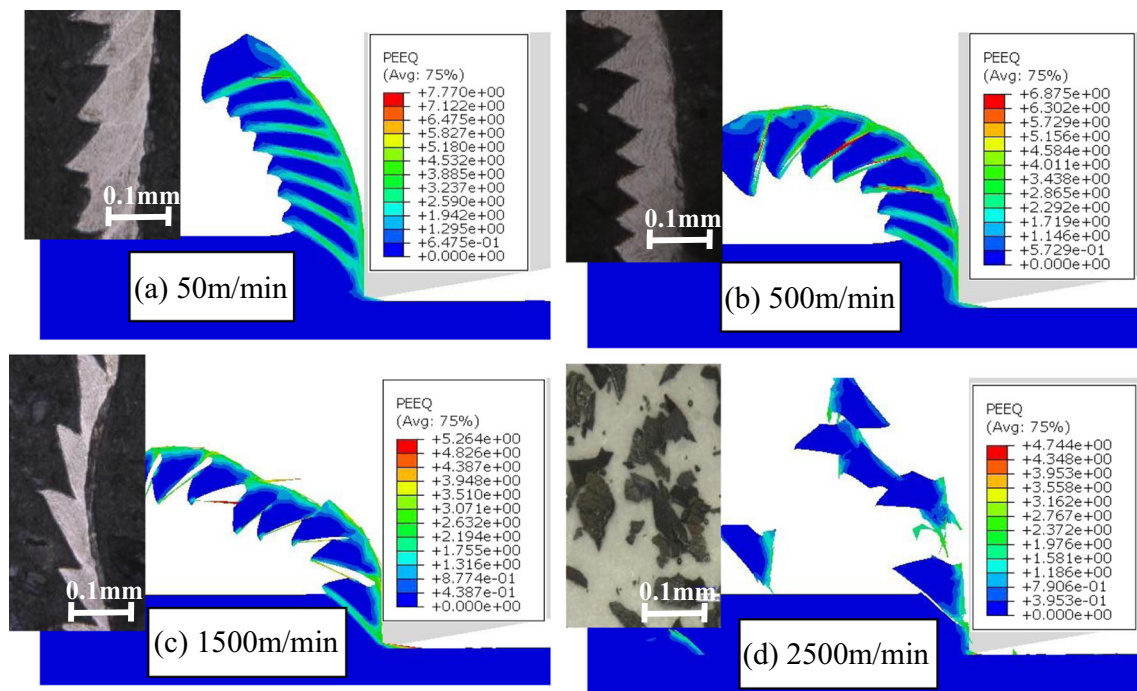


Fig. 5 Schematic of serrated chip formation in orthogonal cutting





**Fig. 6** Variation of chip morphologies under different cutting speeds

where  $h$  is the discontinuous section height (i.e., the vertical distance between the valley and the peak of the serrated section) of serrated chip, and  $H$  is the maximum height of the serrated chip as shown in Fig. 5.

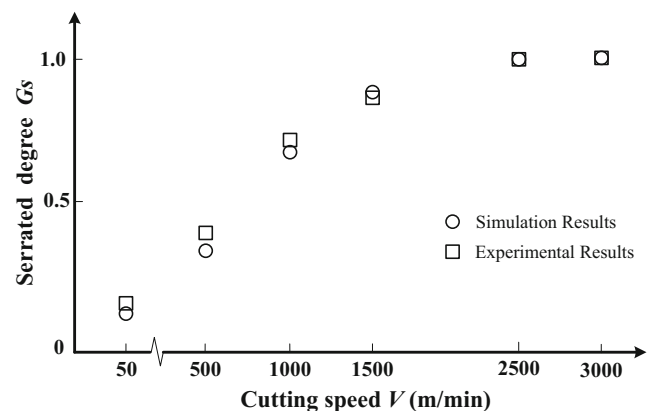
$$f = \frac{V a_c}{d(H-h/2)} \quad (7)$$

where  $d$  is the pitch of two neighboring trapezoids as shown in Fig. 5.

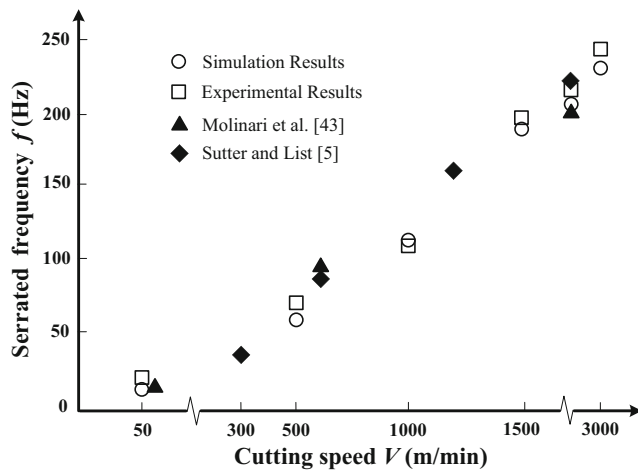
The evolution of chip morphologies with cutting speeds ranging from 50 to 2,500 m/min is presented in Fig. 6, in which the distributions of equivalent plastic strain (PEEQ) can also be seen. As the cutting speed increases, the chip serration is enhanced obviously until the chip morphology evolving to unit at the cutting speed of 2,500 m/min. In the cutting experiments of Ti6Al4V conducted by Sutter and List [5] based on a specific ballistic setup, a chip morphology transition from serrated, more or less regular with localized shearing and possible presence of cracking, to discontinuous at very high speed is also observed. Their results show that the transition speed is 2,700 m/min at the uncut chip thickness of 0.1 mm, which coincides with our results of 2,500 m/min approximately. It can be seen from Fig. 6 that the PEEQ along the primary shear zone and the tool–chip interface (i.e., the secondary shear zone) is larger than that in other areas because the material undergoes severe shear localization in these two positions. Another attractive phenomenon is that the strain in shear zones of serrated chip decreases with the cutting speed

increasing. It can be seen that the highest strain in the PEEQ distributions decreases from 7.770 to 4.744 when the cutting speed increases from 50 to 2,500 m/min. The mechanism to govern this result is that the material property changes from plastic to brittle under higher cutting speed, which has been reported in our previous publications [42]. This mechanism can also explain why the chip evolves from continuous to serrated until it is fractured completely.

Figure 7 shows that the variation of chip serrated degree  $G_s$  under different cutting speeds based on Eq. (6). The serrated degree  $G_s$  has positive correlation with the cutting speed. When the cutting speed reaches 2,500 m/min, the parameter  $G_s$  tends to 1, which means that the adjacent segmentations of serrated chips are separated completely as shown in Fig. 6.

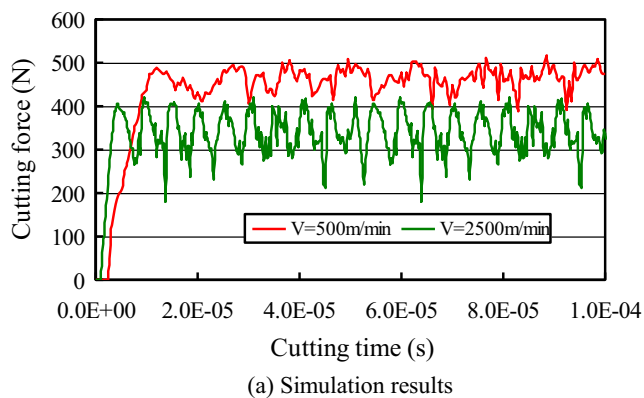


**Fig. 7** Variation of serrated degree under different cutting speeds

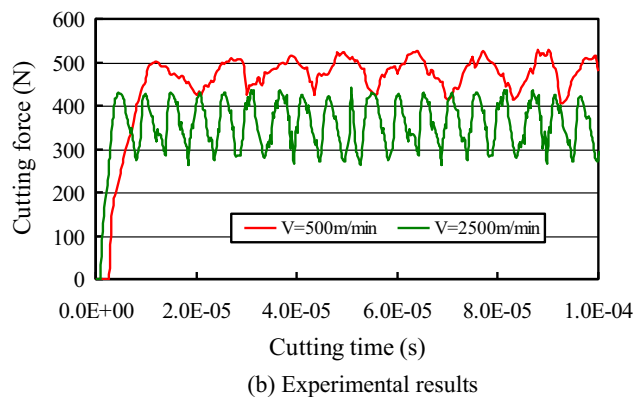


**Fig. 8** Variation of serrated frequency under different cutting speeds [5, 43]

The variation of chip serrated frequency  $f$  under different cutting speeds based on Eq. (7) is illustrated in Fig. 8. It can be seen that the parameter  $f$  increases obviously with the cutting speed increasing. The magnitude of serrated frequency  $f$  in this study matches well with the results obtained by Molinari et al. [43] and Sutter and List [5] as shown in Fig. 8. When the serrated chip evolves to unit ones at the cutting speed of 2,500 m/min, the parameter  $f$  could not be used to describe the chip geometric characteristics.

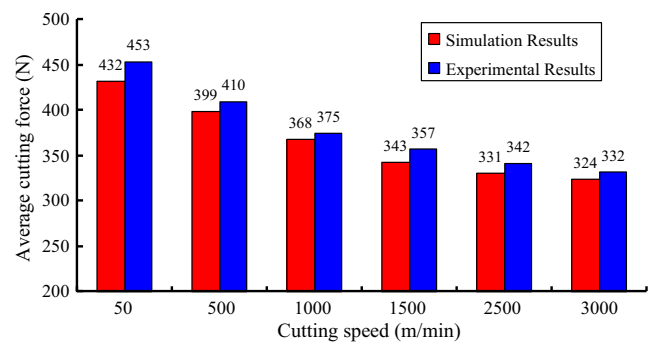


(a) Simulation results



(b) Experimental results

**Fig. 9** Cutting forces under different cutting speeds. **a** Simulation results. **b** Experimental results



**Fig. 10** Comparison of simulation and experimental average cutting forces under different cutting speeds

### 3.3 Analysis of cutting force

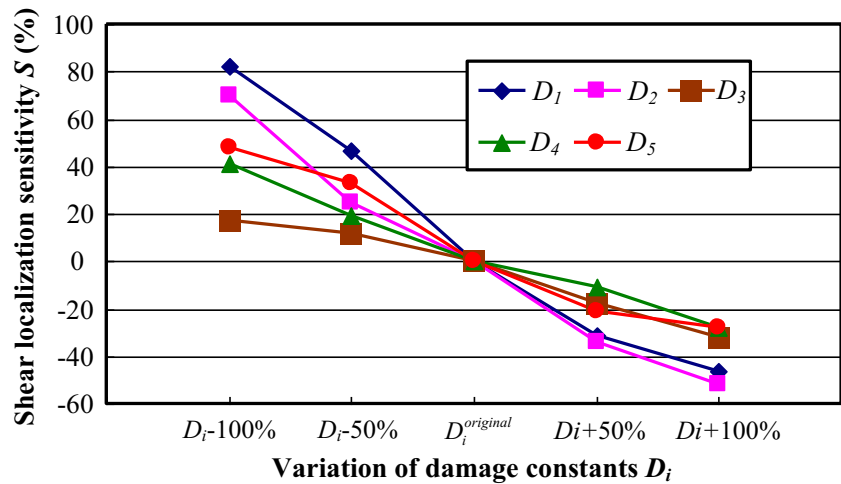
The simulation and experimental cutting forces under different cutting speeds are displayed in Fig. 9. The direction of the cutting force is parallel with  $Y$ -axis as shown in Figs. 2 and 4. It can be seen that the fluctuation occurs due to the cyclic generation of the shear bands in the serrated chips during machining. So, the fluctuant frequencies of cutting force approximate to the ones of chip serration. It can be seen from Fig. 9 that the simulation mean cutting force is 399 N (the experimental mean cutting force is 410 N) with a bandwidth of about 85 N for the cutting speed of 500 m/min. With regard to the cutting speed of 2,500 m/min, the simulation mean cutting force is 331 N (the experimental mean cutting force is 342 N) with a bandwidth of about 130 N. Both fluctuant frequency and amplitude of cutting force under 2,500 m/min are much larger than those under 500 m/min.

The variation of average cutting forces under different cutting speeds has also been analyzed as shown in Fig. 10. The simulation and experimental results of cutting forces are in good comparison. It can be deduced that the cutting force decreases with the cutting speed increasing. It can also be observed from Fig. 10 that the experimental cutting force is larger than that of the simulation results. The main reason lies in that the tool is regarded as sharp in the simulation process in which the cutting edge radius has not been considered. The decrease of cutting force under high cutting speed is a prominent advantage for high-speed machining, which has been widely used for the machining of thin-walled workpieces in aerospace industry.

**Table 5** The researched JC fracture constants for Ti6Al4V

$D_i$	↓100 %	↓50 %	Original	↑50 %	↑100 %
$D_1$	−0.18	−0.135	−0.09	−0.045	0
$D_2$	0	0.125	0.25	0.375	0.5
$D_3$	−1.0	−0.75	−0.5	−0.25	0
$D_4$	0	0.007	0.014	0.021	0.028
$D_5$	0	1.935	3.87	5.805	7.74

**Fig. 11** Shear localization sensitivity of serrated chips to damage constants



#### 4 Shear localization sensitivity of serrated chips to JC fracture constants

As mentioned in Section 2.3, the fracture constants  $D_i$  in Eq. (3) have direct influence on the fracture strain  $\bar{\epsilon}_f$ , which will further determine the chip formation pattern in the cutting process. Considering the complexities of stress state and temperature distribution in the cutting shear zone, it is hard to analyze the influence mechanism of fracture constants on the chip formation mechanism through analytical method, which impels us to solve this problem based on finite element method. Through changing the five fracture constants individually, the serrated degrees of chips are quantitative analyzed, which means that the serrated degree is regarded as the reference parameter.

##### 4.1 Determination of the range for five damage constants $D_i$

The original fracture constants of JC fracture model obtained by experiments [37] have been mentioned in Table 4. In order to investigate the influence of fracture constants on the chip formation in a wide range, the fracture constants are set in the range of decreasing 100 % to increasing 100 % on the basis of original values, with an interval of half of their original values. Table 5 shows the researched JC fracture constants for Ti6Al4V in this study.

##### 4.2 Shear localization sensitivity of serrated chips to the fracture constants

The chip serrated degree is treated as the researched standard in this study. When the fracture constants are changed, the variation of serrated degrees compared to the original result can be analyzed quantitatively. This

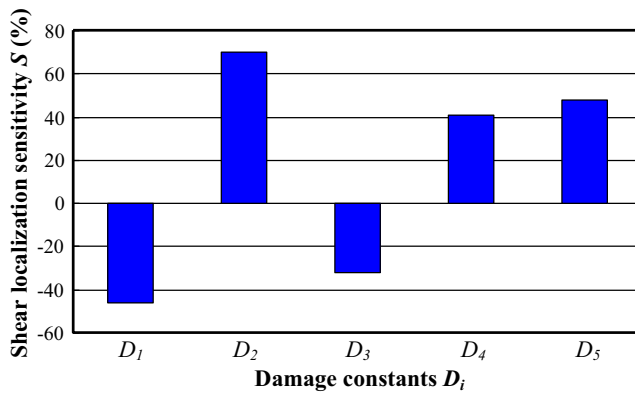
variation  $S$  is defined as the shear localization sensitivity as shown in Eq. (8).

$$S = \frac{G_s^{D_i} - G_s^{original}}{G_s^{original}} \times 100 \% \quad (8)$$

where  $G_s^{D_i}$  is the chip serrated degree under different fracture constants as shown in Table 5 based in Eq. (6), and  $G_s^{original}$  is the chip serrated degree under the original fracture constants based on Eq. (6). The cutting conditions are fixed at the cutting speed of 500 m/min and the uncut chip thickness of 0.1 mm in this section.

Figure 11 presents the shear localization sensitivity  $S$  under different JC fracture constants. It can be seen that when the JC fracture constants decrease, the shear localization sensitivity  $S$  is positive while it is negative when the JC fracture constants increase. The positive value of shear localization sensitivity means the increasing of chip serrated degree and vice versa, which can be attributed to the reason that the fracture strain  $\bar{\epsilon}_f$ , has positive correlation with the five JC fracture constants as shown in Eq. (3). It is shown in Fig. 11 that the effects of JC fracture constants  $D_1$  and  $D_2$  on the shear localization of serrated chips are more conspicuous, no matter promotion or suppression. The effect of parameter  $D_3$  on shear localization is the least apparent, and the parameters  $D_4$  and  $D_5$  fall in between.

When a certain one of JC fracture constants is zero, for example the parameter  $D_5$  is zero, the individual effect of temperature on the shear localization of serrated chip can be obtained. In this way, the individual effects of the initial failure strain, the stress triaxiality, the strain rate, and the temperature on the shear localization can be deduced as shown in Fig. 12. It can be seen that when the parameter  $D_1$  or  $D_3$  is zero, the shear localization is suppressed while the shear localization is promoted when the other three parameters are zero.



**Fig. 12** Shear localization sensitivity of serrated chips when the respective fracture constant  $D_i$  is zero

Furthermore, the shear localization sensitivity is the largest when the parameter  $D_2$  is zero, which illustrates the great influence of stress triaxiality on the chip serration. The analysis of stress state in the cutting shear zone has vital importance on the understanding of chip formation mechanism.

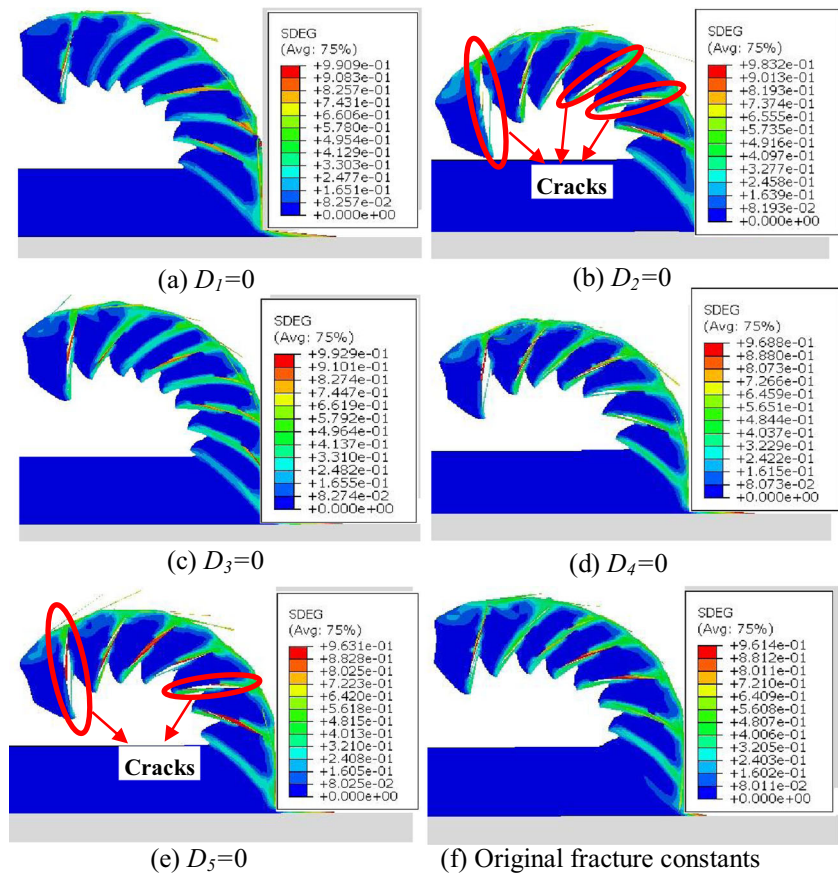
Figure 13a–e shows the distribution of damage variable  $D$  (scalar stiffness degradation, SDEG) of serrated chips when each JC fracture constant is zero, respectively. Figure 13f shows the distribution of damage variable  $D$  under the original JC fracture constants. It can be seen that the value of SDEG is

much less than the failure value (i.e., when damage variable  $D$  equals to 1) when the parameter  $D_1$  or  $D_3$  is zero, so the serrated degree of chip is smaller than that of the original JC fracture constants. In contrast, the value of SDEG in the primary shear zone approaches the failure value which results in the aggravation of chip serration when the parameter  $D_2$  or  $D_5$  is zero. It can be seen from Fig. 13b, e that some adjacent segments nearly separate from each other completely, which are illustrated by the red marks in the figures. Moreover, the bending of the chip is severer due to the degradation of joint strength between adjacent segments.

## 5 Conclusions

The simulation of cutting process can help to get deeper insights into the cutting mechanism. There are two main parts included in this paper. The first one is to carry out the high-speed cutting process of Ti6Al4V with the aid of both simulations and experiments, which gives good accordance covering the chip morphology and cutting force in the two methods. The second one is to investigate the influence of JC fracture constants on the chip formation based on the finite element method, which is the main innovative work conducted in this

**Fig. 13** Distribution of damage variable  $D$  (scalar stiffness degradation, SDEG) under different JC fracture constants





study. Some interesting results have been concluded as follows:

1. Both the simulation and experimental results show that with the cutting speed increasing, the chip serrated degree increases until it tends to one when the chip morphology becomes unit or fragmented. For the orthogonal cutting process of Ti6Al4V, the cutting speed turning point of chip morphology from serrated to unit is about 2,500 m/min.
2. The research shows that the serrated frequency of chips has positive correlation with the cutting speed. When the chip morphology becomes unit, the serrated frequency could not be used to describe the geometric characteristic of chips.
3. With the cutting speed increasing, the mean value of the cutting forces decreases. When the chip morphology evolves from serrated to unit ones under ultra high cutting speed, both the fluctuant frequency and fluctuant amplitudes of the cutting forces increase sharply due to the occurrence of ductile to brittle fracture transition at the chip deformation zone.
4. The shear localization sensitivity is firstly proposed to describe the influence of JC fracture constants on the chip formation process. When the JC fracture constants decrease, the shear localization sensitivity is positive while it is negative when the JC fracture constants increase.
5. The research indicates that the influences of initial failure strain  $D_1$  and exponential factor of stress triaxiality  $D_2$  on the chip formation process are more conspicuous than those of the rest three ones.
6. Through studying the individual effects of the initial failure strain, the stress triaxiality, the strain rate, and the temperature on the shear localization of chips, the conclusion can be drawn that the decreased ranking of effect degree for these variables is the stress triaxiality, the temperature, the initial failure strain, and the strain rate.

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